

DME3051 Mechanical Design

Summary 2

Date: Sep. 13, 2018

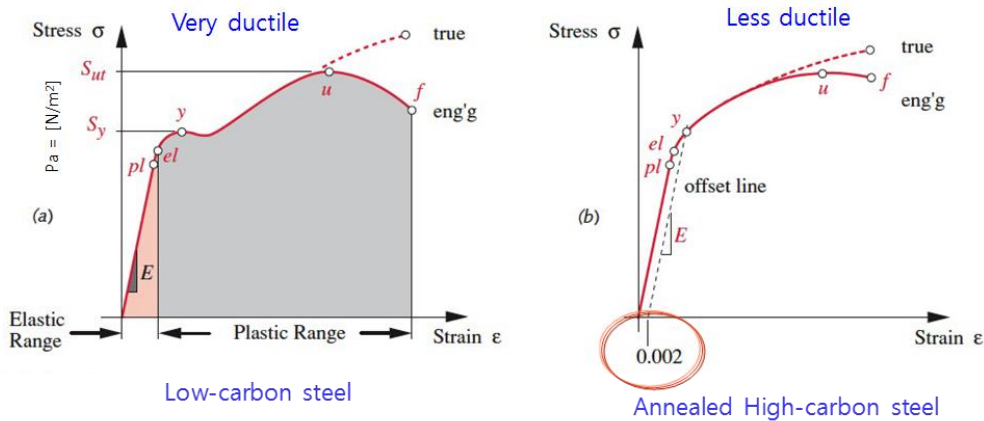
Instructor: Prof. Keun Ryu

Factor of Safety  $N = (\text{Material Strength})/(\text{Design Load})$

Chap. 3 Materials

SEE: Appendix C-1

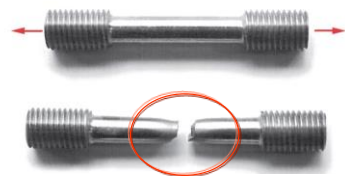
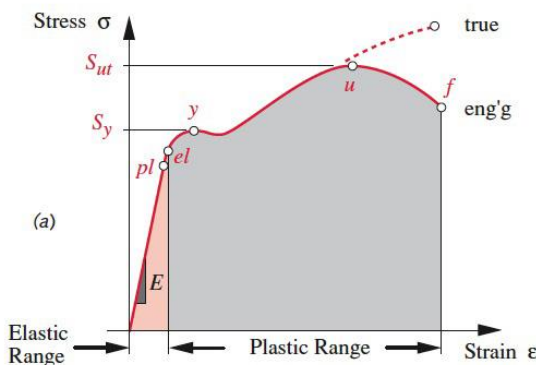
Young's Modulus (E)



- $pl$ : proportional limit
- $el$ : elastic limit  $\rightarrow$  permanent set or plastic deformation;  $el$  and  $pl$  are often the same
- $y$ : Yield point  $\rightarrow S_y$ : yield strength
- $S_{ut}$ : ultimate tensile strength  $\rightarrow$  Largest tensile stress the material can sustain before breaking

Stress drops to fall off to a smaller value at the fracture point

$\rightarrow$  Cause by the "necking-down" or reduction in area of the ductile material.



Non-uniform cross-sectional area

True stress-strain curve: the change in area considered  
 Engineering stress-strain curve: Used in practice

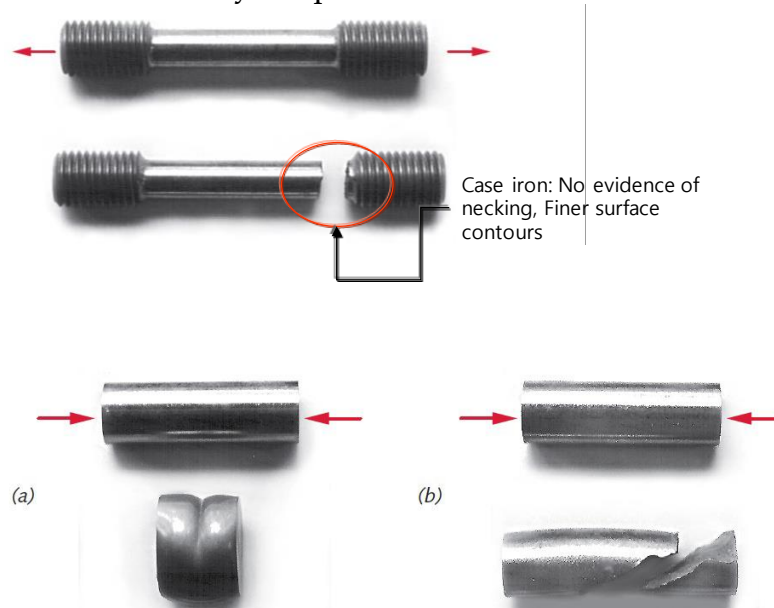
### Ductility:

1. Percent elongation to fracture or percent reduction in area at fracture  
 → Materials with more than 5% elongation at fracture are considered ductile  
 → Most ductile metals have elongations to fracture more than 10%.
2. Tendency for a material to deform significantly before fracturing

**Brittleness:** Absence of significant deformation before fracture

Brittle?

- Lack of a clearly defined yield point and the absence of any plastic range before fracture  
 : Brittle materials do not exhibit a clear yield point.



- Brittle materials proceed to fracture without significant shape change.
- If cracks are present in a ductile material, it can suddenly fracture at nominal stress levels well below the yield strength, even under static loads

### Shear Modulus (G)

Stress-Strain relation for pure torsion

$$\tau = \frac{Gr\theta}{l_0}$$

Labels in the diagram:  
 -  $\tau$ : Shear stress  
 -  $G$ : Shear Modulus or Modulus of rigidity  
 -  $r$ : Radius of specimen  
 -  $\theta$ : Angular twist in radian  
 -  $l_0$ : Original gauge length

**G: Shear Modulus or Modulus of rigidity**

G can be defined in terms of E and  $\nu$

Poisson's ratio: Ratio between lateral and longitudinal strain.  $\sim 0.3$  (Most metal)

$$G = \frac{E}{2(1+\nu)}$$

**Poisson's ratio:** Ratio of the proportional decrease in a lateral measurement to the proportional increase in length in a sample of material that is elastically stretched.

→ The transverse contraction during a tensile test is related to the longitudinal elongation.

$$\varepsilon_x = \frac{\sigma_x}{E}$$

$$\varepsilon_y = \varepsilon_z = -\frac{\nu\sigma_x}{E}$$

$$\nu = \frac{\left| \frac{\varepsilon_y}{\varepsilon_x} \right|}{\left| \frac{\varepsilon_z}{\varepsilon_x} \right|}$$

- **Toughness:** Ability of a material to absorb energy per unit volume without fracture [in-lbf/in<sup>3</sup> or J/m<sup>3</sup>] → Charpy IMPACT TEST.

- **Fracture toughness  $K_{Ic}$ :** A material property that defines its ability to resist stress at the tip of a crack. Measured by subjecting a standardized, pre-cracked test specimen to cyclical tensile loads until it breaks.